# Under the Hood of the Quantum Computer

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# Speaker

- Seventeen years with Hewlett Packard
  - Software/hardware/firmware/chip design, embedded systems design
  - Microprocessor and ASIC emulation R&D leadership
- Three with Synopsys, top EDA supplier
  - Tools for chip design
- Three more with Rudolph and KLA-Tencor, top suppliers in semiconductor wafer inspection
  - Rudolph for broadband visual macro inspection of individual die
  - K-T for UV-laser dark field inspection of wafers
- University dean for computer science at Colorado Tech
  - Doctoral student did his dissertation on quantum computing
- Professor and program director for cybersecurity and data science at the University of Denver
  - Masters student doing independent research on quantum computing

#### Outline of the Talk

- Background and motivation of the talk
- What is quantum computing
- Quantum computing history
- Recent developments
- Quantum computing under the hood
- Implications to cyber security (cryptanalysis)
- Mitigation

# Background and Motivation

- A quantum computer, if it existed, would seriously threaten RSA encryption. This is via Peter Shor's algorithm
- Research has been under way since 1980s
- Photon polarization and/or electron spin could enable
- Several companies claim to have on
- Hence the urgency

# What's the Fuss: D-Wave, USC/LMC, NASA/Google

- 2011 D-Wave Systems made a chip-set and system: 128 qubit, to be homed at USC Lockheed Martin Quantum Computing Ctr
- Much criticized by academics; later published in *Nature*
- 2013 Google to form Quantum AI Lab at NASA

Ames: 512 qubit sys from D-Wave

# History of Quantum Computing

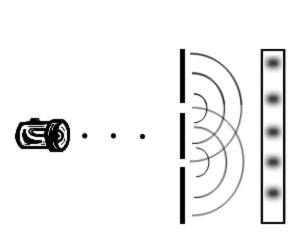
- Quantum mechanics since early 20<sup>th</sup> Century: Einstein, Bohr, Planck, Dirac, Heisenberg, Schrodinger (remember the cat), et al
- One cannot know both the position and the momentum of a particle (Heisenberg)
- A photon can be in two places at once
- Digital computing since WW II era
- Quantum computing conceived in 1980s
  - Yuri Manin (1980), Richard Feynman (1982)
  - David Deutsch (1985)
  - Peter Shor (1994)

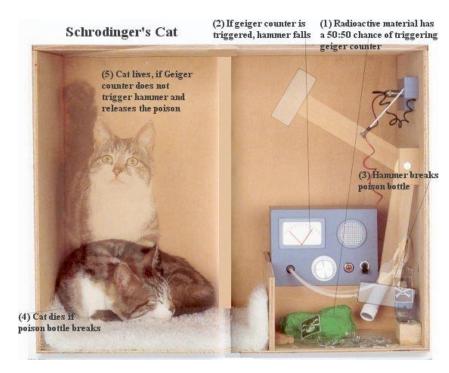
### From Quantum Mechanics

- Discrete (from the latin quanta)
- "we cannot know the precise position and momentum of a quantum particle at the same time"
- Superposition
  - Heisenberg's Principle (uncertainty)
    - Schrodinger's cat, for example
  - One cannot know the state without testing
    - Thus invalidating or interfering
    - Results in a "collapse" to the measured state
- Entanglement: One knows only the aggregate; the individual properties are not known: "spooky action at a distance" -Einstein

# Two-slit experiment; the cat

- Even single photon emission produces wave constructive and destructive interference
- Schrodinger's cat is both alive and dead!?

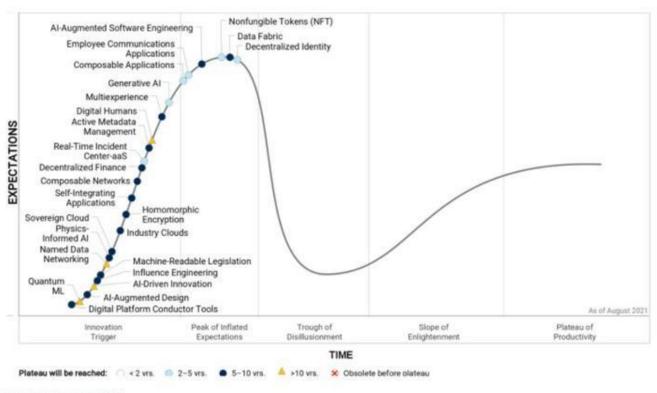




# **Applications**

- Finding factors of large composite integers
- Al and machine learning
- Computational chemistry, biology
- Drug design
- Weather forecasting
- Optimization
- Financial modeling

# QC makes it to the



Source: Gartner (August 2021)

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Source: Gartner (August 2021)

# Quantum supremacy in 2019?

 Hello quantum world! Google publishes landmark quantum supremacy claim (nature.com)

### **Variations**

- Quantum circuit model (most often used)
- Quantum Turing machine
- Adiabatic quantum computer
- One-way quantum computer

# Exploitation

- If the details may be hidden by "entanglement", we may exploit that
- In a manner similar to how the discrete (fast)
   Fourier Transform is able to exploit properties of the interplay between complex numbers and the periodicity of the exponential function
- Superposition
- The lack of detailed knowledge of the system may enable fast computation
- Measurement alters the system, and that can be exploited to detect eavesdropping

### Under the hood

- Notation will be Dirac from Mermin
  - Cbit, Qbit, |0>, |1>,  $|\phi>$
- Qbit is superposition as follows

$$|\psi\rangle = \alpha_0 |0\rangle + \alpha_1 |1\rangle = \begin{bmatrix} \alpha_0 \\ \alpha_1 \end{bmatrix}$$

$$|\alpha_0|^2 + |\alpha_1|^2 = 1$$
,  $\alpha_i$  complex numbers

- One Qbit demands 2-vector space
- Two Qbit demands 4-vector space
- $|\alpha_0|^2$  is probability assoc. with |0>

# Cbits are Qbits, too

$$|0\rangle = \begin{bmatrix} 1+0i \\ 0 \end{bmatrix} = \begin{bmatrix} 1 \\ 0 \end{bmatrix}$$

$$|1\rangle = \begin{bmatrix} 0 \\ 1 + 0i \end{bmatrix} = \begin{bmatrix} 0 \\ 1 \end{bmatrix}$$

#### Issues

- Noise
- Decoherence
  - Error correction
- Extreme cold required
- Multiple runs of the same program

# Programming it

- List of QC simulators | Quantiki
- Quantum compiler with libraries
- C++, Python, Java, several others
- Simulate on a classical computer
- Assembly language metaphor
- Analogy to signal flow graphs or digital logic circuits
- Brilliant.com has a course in programming QC

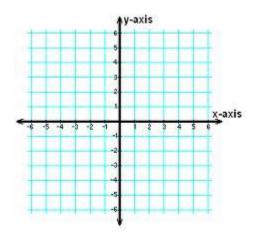
# QC programming is open source

 <u>Cambridge Quantum makes TKET SDK open</u> <u>source (msn.com)</u>

$$|\mathbf{0}\rangle = \begin{bmatrix} 1 & 0 & 0i \\ 1 & +00i \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \end{bmatrix}$$

### More on Qbits

- Computation basis (bases)
- $|0\rangle$  is  $\binom{1}{0}$ ,  $|1\rangle$  is  $\binom{0}{1}$



- We use orthonormal set of vectors for bases
- 2-Qbit uses 4-vector spaces

$$|\psi\rangle = \alpha_0 |00\rangle + \alpha_1 |01\rangle + \alpha_2 |10\rangle + \alpha_3 |11\rangle = \begin{vmatrix} \alpha_0 \\ \alpha_1 \\ \alpha_2 \\ \alpha_3 \end{vmatrix}$$

- Generally one uses only 1 & 2-Qbits
- "A vector space of 2 or 4 dimensions over the complex numbers"

### **Architecture**

- Input register of Qbits
- Output register of Qbits
- Logic in between is formed from Qbits
- Logic blocks are restricted to reversible, unitary transformations, designed to exploit properties
- Measurement blocks are irreversible and are used to get final answer only
- Final answer is a "collapse" based on probability

### Clarifications

- Note matrix notation for transformations
- Reversible means the inputs can be determined by putting the outputs through the same transformation in reverse
- A unitary matrix as a transformation means that the inner product of the vector is preserved. The conjugate transpose equals the inverse.

# Very brief review of linear algebra

A square matrix can transform a column vector

Such matrices can be cascaded

- Such a matrix is orthogonal if the L2 norm of each row and column is 1
- For example [[cos(theta), -sin(theta)],
  - [sin(theta), cos(theta)]] will rotate the vector by theta

### Operators

- Exclusive OR
- Inner product
- Complex conjugation
- Linear, reversible, unitary transformations via matrices
- Matrix multiplication

$$|q_0\rangle - I - \theta$$

# Common logic blocks

- **X,** NOT, negates, uses  $\begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$
- $C_{i,j}$ , controlled NOT, if i==1 it negates, else no-op
- **S,** swap operator
- **Z**, uses  $\begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}$
- **H**, Hadamard, uses  $\frac{1}{\sqrt{2}}(X + Z)$
- M, measurement, not reversible

# Single-qubit quantum gates

• Hadamard H = 
$$\frac{1}{\sqrt{2}} \begin{vmatrix} 1 & 1 \\ 1 & -1 \end{vmatrix}$$

• Not 
$$X = \begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix}$$

• 
$$Z = \begin{bmatrix} 1 & 0 \\ 0 & -1 \end{bmatrix}$$

• Identity I = HH = 
$$\begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$$

# Methodology

- Input and output "kets" of qubits
- Signal flow diagrams
- 2<sup>n</sup> = size of the alpha vector

# Peter Shor's Algorithm

- Used to determine the period r associated with RSA, N=pq, b(x+r)=b(x)
- That, along with public key N, is enough to enable the tractable determination of the private key pq, which then breaks RSA
- Uses the quantum Fourier Transform, a quantum variant of the DFT/FFT
- Plus numerous number theory tricks
- Polynomial time vs. exponential time

# Polynomial vs. exponential time

n	n^3	10^n
10	1000	1.00E+10
100	1.00E+06	1.00E+100
1000	1.00E+09	1E+1000
10000	1.00E+12	1E+10000

#### **RSA**

- Bob wants to receive from Alice; he knows N=pq and passes her only N and c; cd=1 mod (p-1)(q-1)
- Alice sends encoded msg  $b=a^c \mod(N)$  which Bob can decode
  - $-a=b^d \mod(N)$
- Eve can only intercept and decode if she knows p or q

### More Shor

- But if one could find the period r of the encoded msg b, one could directly decode b
- Roadmap: Use Shor to get r then use classical computer to find d to decode b

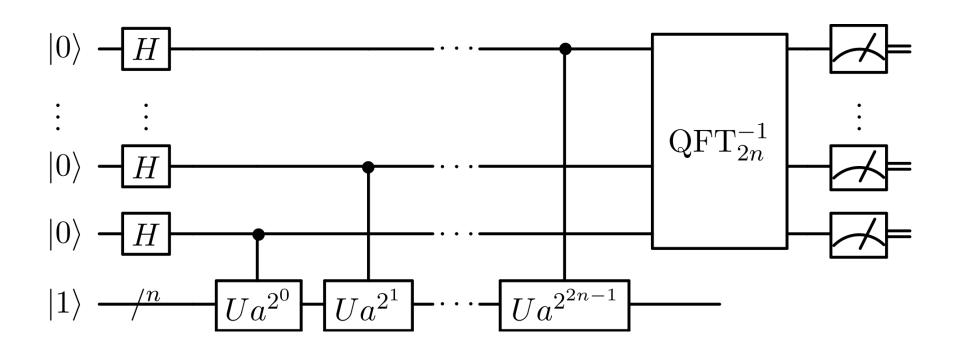
### Quantum Fourier Transform

- $U_{FT} = H_3(V_{32}H_2)(V_{31}V_{21}H_1)(V_{30}V_{20}V_{10}H_0)P$
- Where P permutes the basis and
- $\boldsymbol{V}_{i,j} = \exp(i\pi\boldsymbol{n}_i\boldsymbol{n}_j/2^{|i-j|})$
- $n_i$  is projection onto state i

### More Shor

- $oldsymbol{U}_{FT}$  is then applied to input register
- The output register is all we need from the quantum computer
- Number theory trick applied on conventional computer to get period r and then d
- Conventional computer then decodes b

### Shor's



### Mermin on Shor's

Wayback Machine (archive.org)

#### D-Wave and IBM

- http://www.networkworld.com/news/2011/092611quantum-computing-250825.html?source=NWWNLE nlt daily am 2011-09-26
- IMHO: It is a good start but far from what would be needed for Shor's
- http://www.networkworld.com/community/blog/ibmscientists-discuss-quantum-computingbreakthrough?source=NWWNLE\_nlt\_daily\_am\_2012-02-28
- IBM's Experimental Quantum Computing Lab approach described above

# Mitigation?

- NIST is running a competition for it
- Post-Quantum Cryptography | CSRC (nist.gov)
- Post-Quantum Cryptography | CSRC (nist.gov)
- Quantum key distribution (QKD)
  - Polarized photons are used
- Post-quantum cryptography
- True randomness via quantum mechanics
- [2106.06640] Quantum-resistance in blockchain networks (arxiv.org)

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